The paradox that four equals five

In a broadcast, I once quoted, as an obvious truth, "two and two are four". Shortly afterwards I had an indignant letter from a gentleman who asserted that 4 was equal to 5 – and sent me a 'proof' of this!

Here it is, starting with

$$16 - 36 = 25 - 45$$

Adding 81/4 to each side

$$16 - 36 + 81/4 = 25 - 45 + 81/4$$

ie
$$(4 - 9/2)^2 = (5 - 9/2)^2$$

so
$$4 = 5$$

Can you find the slip in it?